# A General Theory of Tax Smoothing by Anastasios G. Karantounias

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## What the Paper Does

- Optimal labor taxation with complete markets or only real risk-free debt
- With commitment or smooth MPE
- With general recursive preferences (risk sensitivity etc.)

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Optimal taxation is determined by two forces:

- Equalize marginal distortions over time: cost of raising an extra dollar in taxes should be as constant as possible
- Asset price manipulation: reduce required PV of taxes by minimizing the value of gov't debt

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Making the Theory More General...

- Multi-period debt
- Other market incompleteness
- (Heterogeneous agents)

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## A Textbook Example

• Preferences:

$$E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{c_t^{1-\sigma}}{1-\sigma} - \frac{\ell_t^{1+\psi}}{1+\psi} \right]$$

• Initial debt: *b*<sub>t</sub>

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## Ramsey first-order conditions

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$$c_t^{-\sigma}[1+\Phi(1-\sigma)]+\sigma\Phi b_t=\mu_t$$

$$\ell_t^{\psi}[1 + \Phi(1 + \psi)] = \mu_t$$

- Φ: cost of raising an extra unit in taxes (constant over time and across states); numeraire: good weighted by marginal utility
- $\mu_t$ : LM on resource constraint (benefit of marginal expansion in the production frontier)

$$\tau_t = 1 - \frac{\ell_t^\psi}{c_t^{-\sigma}}$$

How does this paper go beyond the textbook example?

- In Non-state separable preferences
- Only risk free debt
- Ommitment vs. no commitment

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#### Non-state separable preferences

- Increasing the level of utility in state  $s^t$  affects the value of resources in state  $\tilde{s}^t$
- Value in manipulating utility levels, even at the cost of increasing tax distortions

$$\frac{1}{\Phi_{t+1}} = \frac{1}{\Phi_t} - \eta_{t+1}$$

 η<sub>t+1</sub>: martingale difference (in the appropriate measure), related to the value of debt across states

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Only risk-free debt (AMSS 2002)

- Cannot perfectly smooth distortions across states
- New link across different histories: value of debt at t measurable wrt t-1 info
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$$E_t u_{c t+1} \Phi_{t+1} = u_{ct} \Phi_t.$$

Paper provides expression that combines this and non-state separable utility

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Generalize to arbitrary debt payoffs (BEGS, 2017 and 2021)

• Exogenously given state-contingent payoff  $x(s^t|s^{t-1})$ 

$$E_t\left[\frac{u_{c\,t+1}\Phi_{t+1}}{x(s^{t+1}|s^t)}\right] = u_{ct}\Phi_t E_t\left[\frac{1}{x(s^{t+1}|s^t)}\right]$$

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# Time-consistency

- Desire to devalue initial debt propagates over time
- With one-period debt: incentive to increase debt  $(\Phi_t)$

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# Heterogeneity

- Multiple implementability constraints:
  - Marginal value of redistributing from agent i to agent j
  - Marginal value of redistributing from agent *i* to government
- Bassetto (2013), BEGS (2017b, 2021)

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# Conclusion

- Deep insights
- Can push to even more generality
- Show two guiding principles across them

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